## ME 755

## SPECIAL FUNCTIONS & APPLIED DIFFERENTIAL EQUATIONS

## Winter 2004

Instructor: Richard Culham E3-2133J ext. 3839 Email: rix@mhtlab.uwaterloo.ca

Recommended: Handbook of Mathematical Functions with Formulas, Graphs, and, Mathematical Tables, Edited by Milton Abramowitz and Irene Stegun,

9th Printing, Dover Publications, New York, 1972.

Supplementary see reference list for each section

Objective: Introduce students to a wide range of special mathematical functions found

in engineering applications. The course will examine analytical formulations and relationships used to determine these special functions. Given the power and accessibility of computer algebra tools such as Maple and Mathematica, we will also explore the use of these powerful software programs to solve a range of problems from simple to complex.

Outline: 1. General Introduction

2. Introduction to Computer Algebra Systems

3. Factorial, Gamma and Beta Functions

4. Error and Complimentary Error Functions

5. Elliptic Integrals, Theta Functions and Elliptic Functions

6. Bessel Functions of the First and Second Kind

7. Legendre Polynomials and Functions

8. Chebyshev Polynomials

9. Hypergeometric Functions

## **Assignments**:

Five problems sets will be assigned. Each problem set must be completed using a computer algebra tool of your choice. Given the availability of Maple on the University wide computer network, I fully expect that most people will choose to you this for their assignments. This course is designed to provide an opportunity for students to explore algebraic, symbolic and numerical methods used to solve engineering problems. While the assigned problems may appear to be straight forward in some instances, I encourage you to provide as much detail, including plots, secondary proofs and any other material that provides insight into the assigned problems.

Assessment:	Assignment #1:	Gamma and Beta Functions	20%
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Due Date: January 29, 2004

Assignment #2: Error and Complementary Error Functions 20%

Due Date: February 12, 2004

Assignment #3: Elliptic Integrals and Elliptic Functions 20%

Due Date: February 26, 2004

Assignment #4: Bessel Functions 20%

Due Date: March 11, 2004

Assignment #5: Legendre Functions and Chebyshev Polynomials 20%

Due Date: March 25, 2004