



Thermal Resistance-Based Bounds for the Effective Conductivity of Composite Thermal Interface Materials

P. Karayacoubian, M. M. Yovanovich, and J. R. Culham

Microelectronics Heat Transfer Laboratory
Department of Mechanical Engineering
University of Waterloo
Ontario, Canada

Outline

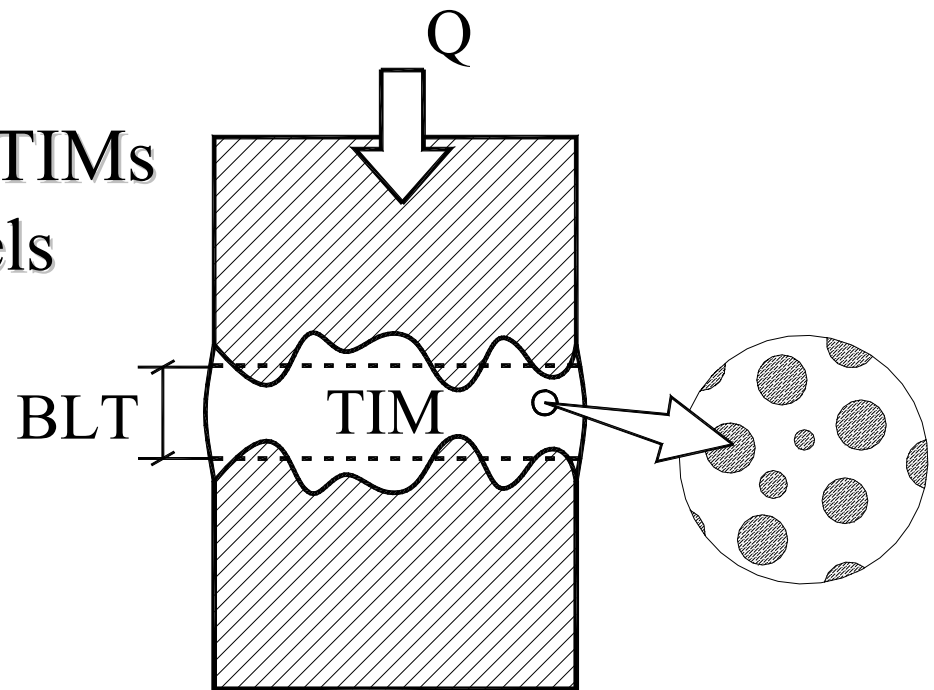


- Motivation
- Problem statement
- Model development
- Numerical and experimental validation
- Conclusions
- Future work

Motivation



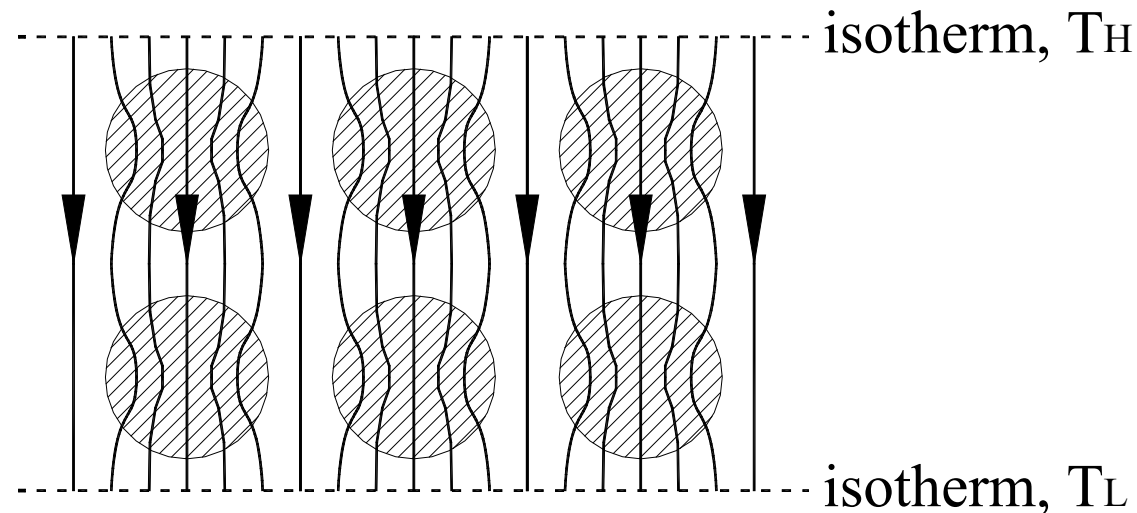
- Thermally enhanced greases used as thermal interface materials (TIMs) in microelectronics cooling applications
- Thermal resistance, R , of TIMs required for thermal models
- $R = R(k_e, BLT, R_{\text{contact}})$



Problem Statement



- To develop analytical models for effective thermal conductivity of fluidic composite materials
- Account for particle-particle interactions → good agreement for high and low particle volume fractions (Φ)



Model: Assumptions

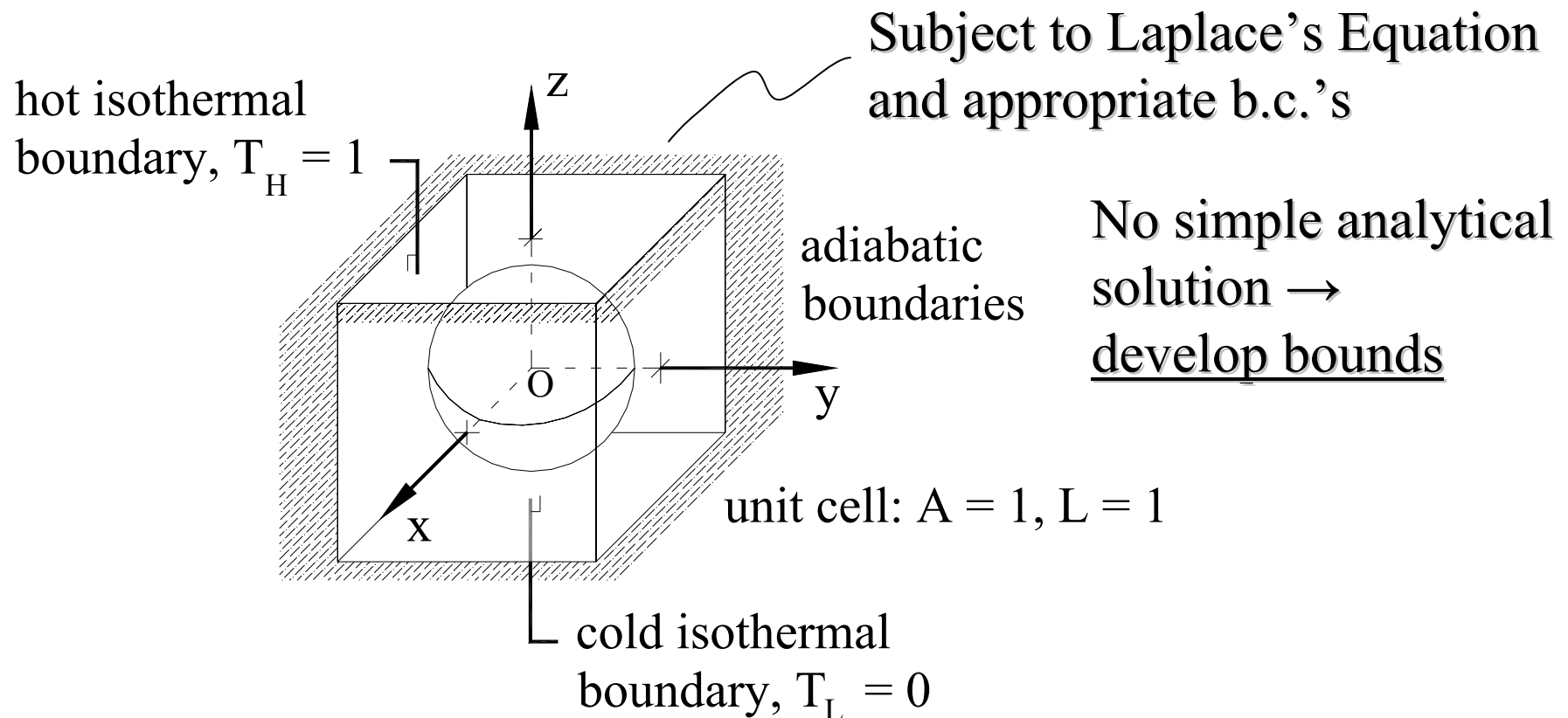


1. N uniform spherical particles, $N \gg 1$
2. arranged in cubic lattice with
3. perfect thermal contact between phases and
4. isotropic and constant thermal conductivities

Model: Characteristic Cell



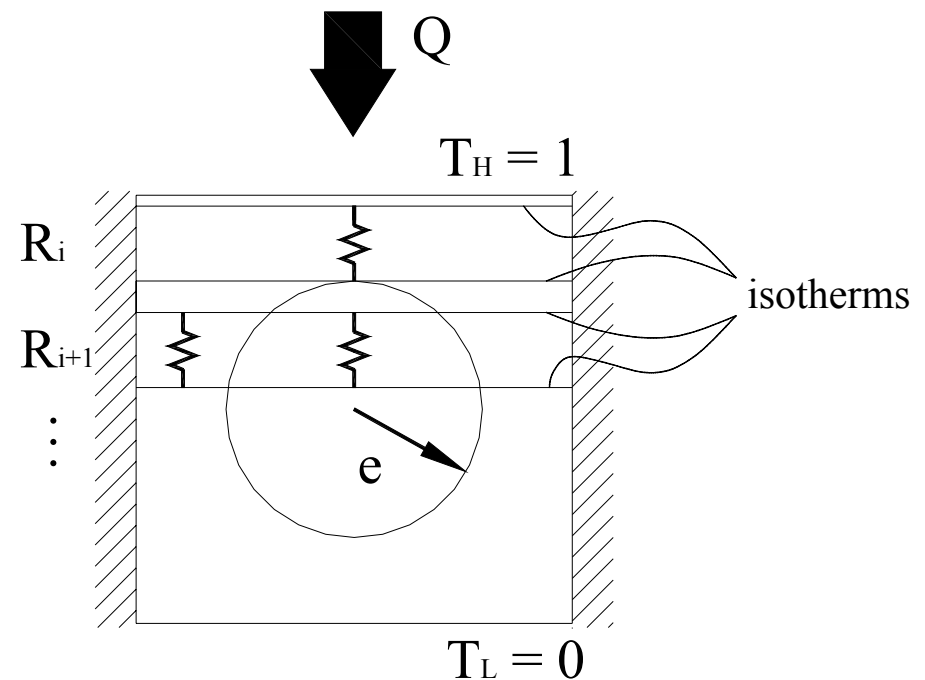
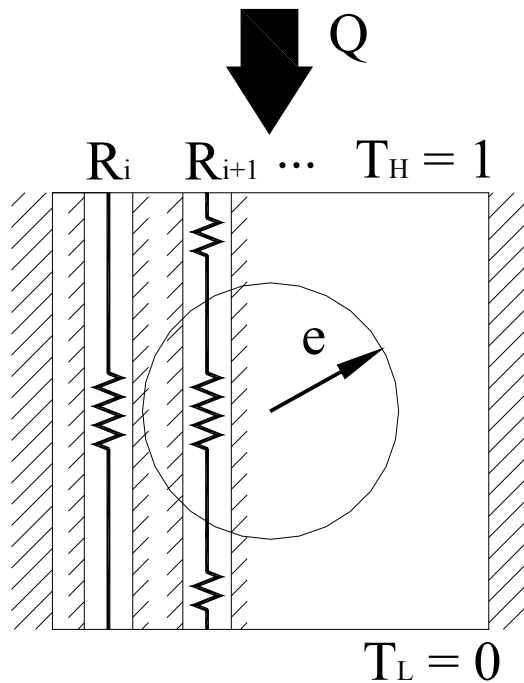
- The assumptions allow one to consider a *characteristic cell*



Model: Bounds



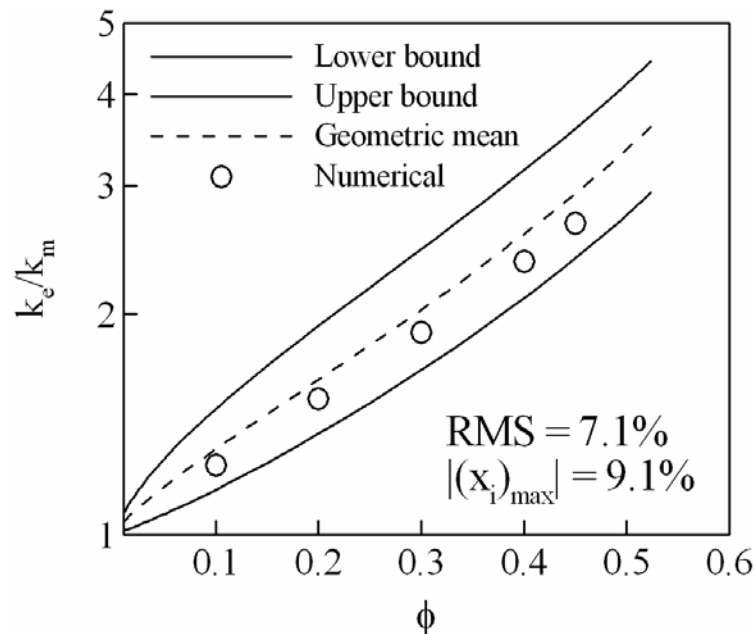
- Lower bound on k_e : Parallel adiabats
- Upper bound on k_e : Perpendicular isotherms



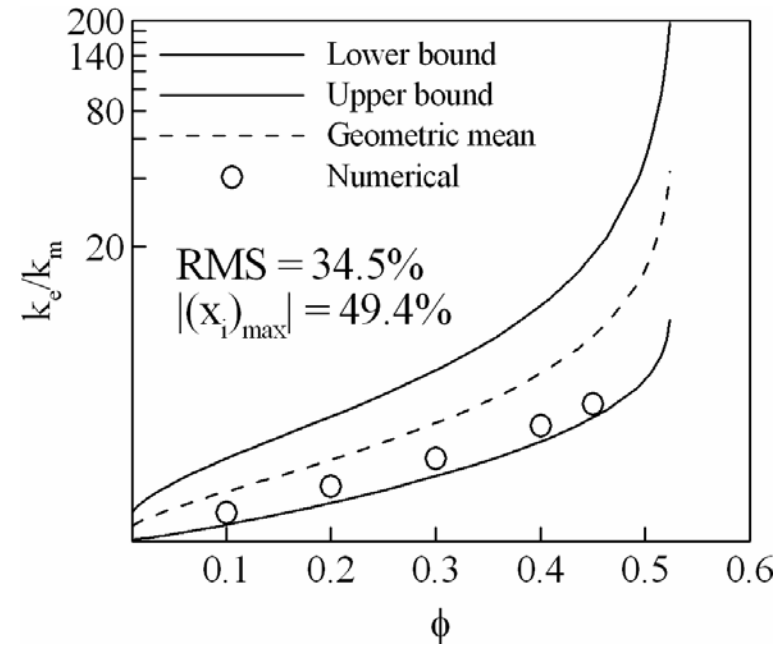
Numerical Results



- Model validated for
Volume fractions, $\Phi = 0.1, 0.2, 0.3, 0.4, 0.45$
Conductivity ratios, $\kappa = 10, 100, 1000$



$\kappa = 10$



$\kappa = 1000$

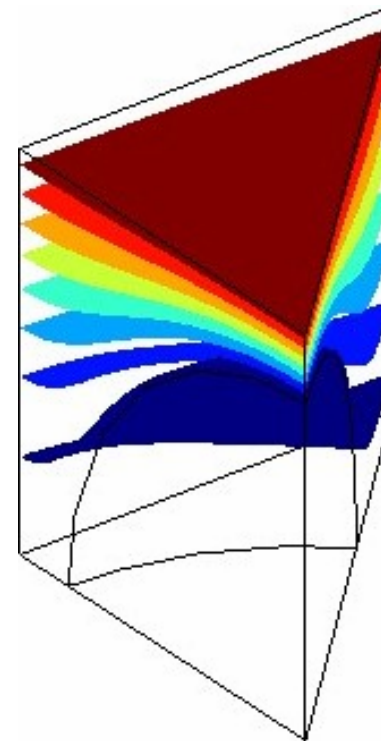
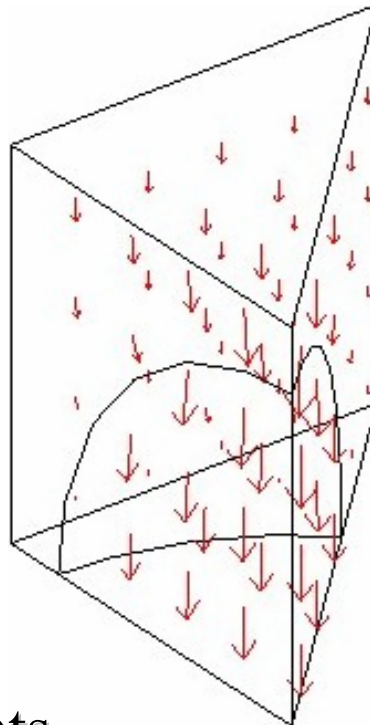
Numerical Results (cont'd)



- Geometric mean of bounds gives good agreement
- Physically, adiabats are neither parallel nor isotherms perpendicular, though numerical results indicate parallel adiabats more realistic

$$\Phi = 0.3$$

$$\kappa = 100$$

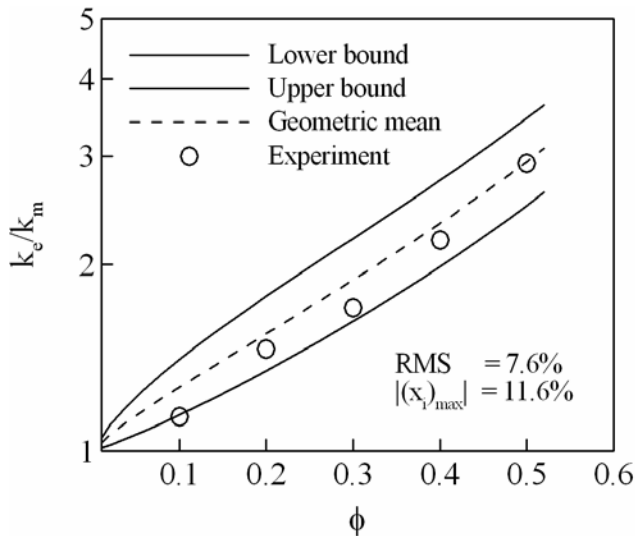


1/16th cell, ~ 50K elements

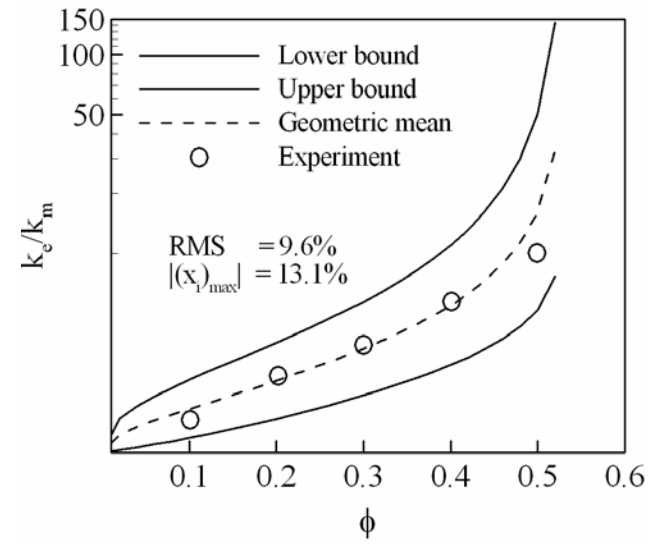
Experimental Results



- Model validated with experimental data in literature
- Geometric mean gives very good agreement, even when particles are irregular (non-spherical)

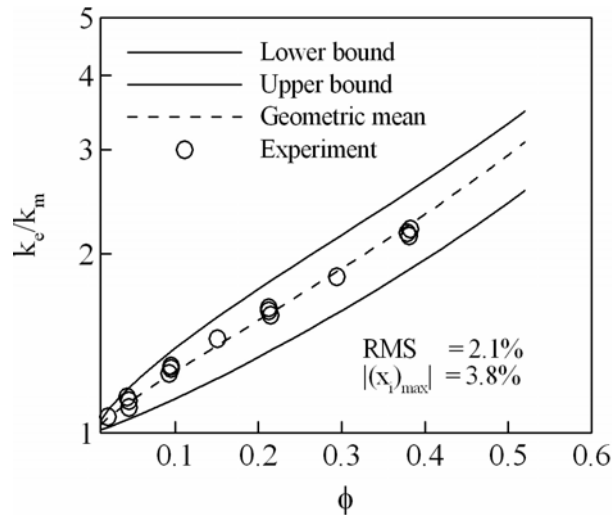


$\kappa = 7.7$
silica, epoxy
spherical



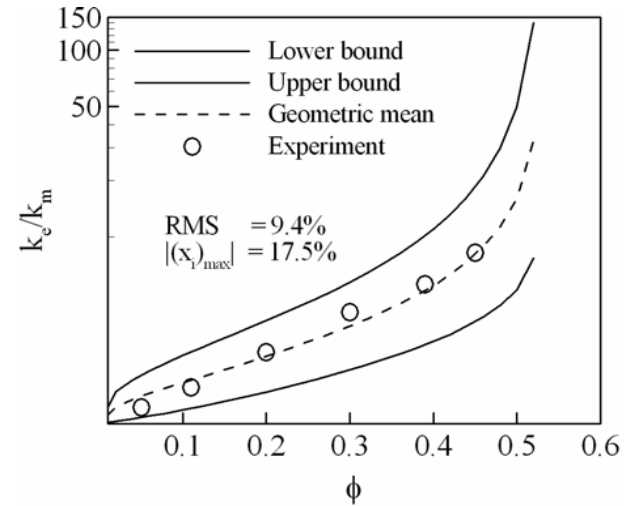
$\kappa = 1128$
silica-coated Al nitride, epoxy
highly irregular

Experimental Results (cont'd)

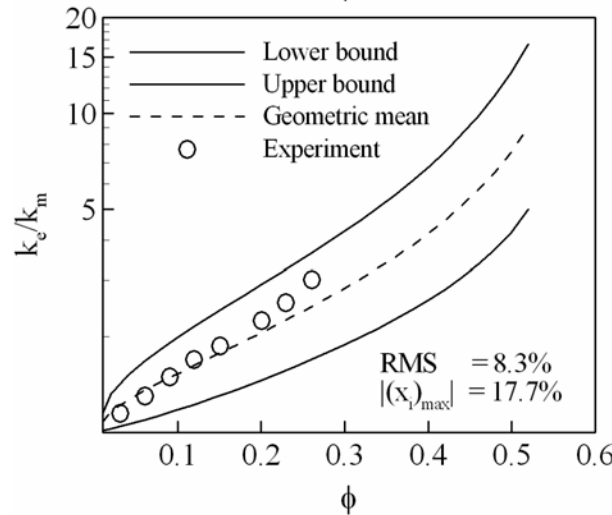


(a)

(b)



(c)



- (a) $\kappa = 7.7$; silica, epoxy; spherical¹
- (b) $\kappa = 41.7$; Al_2O_3 , epoxy; irregular²
- (c) $\kappa = 51.7$; Al_2O_3 , epoxy; irregular³

¹(Sundstrom and Chen, 1970)

²(Lin, Bhatia, and Ford, 1993)

³(Tavman, 2000)

Summary and Conclusions



Model gives very good agreement with

(i) Numerical results

- Model consistently overpredicts numerical results
- Parallel adiabats more realistic model

(ii) Experimental results

- Even when particles are irregular

$$0.1 \leq \Phi \leq 0.45$$

$$10 \leq \kappa \leq 1000$$

Future Work



Extend the present analysis to

1. a general rectangular lattice arrangement → particle distribution,
2. various particle geometries (e.g. ellipsoids, prismoids, right circular cylinders, etc.) → particle alignment, and
3. imperfect thermal contact between particle and matrix (e.g. oxides)

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