

5-84 A cylinder equipped with a set of stops for the piston is initially filled with air at a specified state. Heat is transferred to the air until the volume doubled. The work done by the air and the amount of heat transfer are to be determined, and the process is to be shown on a P - v diagram.

Assumptions **1** Air is an ideal gas with variable specific heats. **2** The kinetic and potential energy changes are negligible, $\Delta ke \cong \Delta pe \cong 0$. **3** The thermal energy stored in the cylinder itself is negligible. **4** The compression or expansion process is quasi-equilibrium.

Properties The gas constant of air is $R = 0.287 \text{ kPa} \cdot \text{m}^3/\text{kg} \cdot \text{K}$ (Table A-1).

Analysis We take the air in the cylinder as the system. This is a closed system since no mass crosses the boundary of the system. The energy balance for this closed system can be expressed as

$$\underbrace{E_{\text{in}} - E_{\text{out}}}_{\text{Net energy transfer by heat, work, and mass}} = \underbrace{\Delta E_{\text{system}}}_{\text{Change in internal, kinetic, potential, etc. energies}}$$

$$Q_{\text{in}} - W_{\text{b,out}} = \Delta U = m(u_3 - u_1)$$

$$Q_{\text{in}} = m(u_3 - u_1) + W_{\text{b,out}}$$

The initial and the final volumes and the final temperature of air are

$$v_1 = \frac{mRT_1}{P_1} = \frac{(3 \text{ kg})(0.287 \text{ kPa} \cdot \text{m}^3/\text{kg} \cdot \text{K})(300 \text{ K})}{200 \text{ kPa}} = 1.29 \text{ m}^3$$

$$v_3 = 2v_1 = 2 \times 1.29 = 2.58 \text{ m}^3$$

$$\frac{P_1 v_1}{T_1} = \frac{P_3 v_3}{T_3} \longrightarrow T_3 = \frac{P_3}{P_1} \frac{v_3}{v_1} T_1 = \frac{400 \text{ kPa}}{200 \text{ kPa}} \times 2 \times (300 \text{ K}) = 1200 \text{ K}$$

No work is done during process 1-2 since $v_1 = v_2$. The pressure remains constant during process 2-3 and the work done during this process is

$$W_{\text{b,out}} = \int_1^2 P dv = P_2(v_3 - v_2) = (400 \text{ kPa})(2.58 - 1.29) \text{ m}^3 = \mathbf{516 \text{ kJ}}$$

The initial and final internal energies of air are (Table A-21)

$$u_1 = u_{@300 \text{ K}} = 214.07 \text{ kJ/kg}$$

$$u_3 = u_{@1200 \text{ K}} = 933.33 \text{ kJ/kg}$$

Then from the energy balance,

$$Q_{\text{in}} = (3 \text{ kg})(933.33 - 214.07) \text{ kJ/kg} + 516 \text{ kJ} = \mathbf{2674 \text{ kJ}}$$

Alternative solution The specific heat of air at the average temperature of $T_{\text{avg}} = (300 + 1200)/2 = 750 \text{ K}$ is, from Table A-2b, $c_{v,\text{avg}} = 0.800 \text{ kJ/kg} \cdot \text{K}$. Substituting,

$$Q_{\text{in}} = m(u_3 - u_1) + W_{\text{b,out}} \cong mc_v(T_3 - T_1) + W_{\text{b,out}}$$

$$Q_{\text{in}} = (3 \text{ kg})(0.800 \text{ kJ/kg} \cdot \text{K})(1200 - 300) \text{ K} + 516 \text{ kJ} = \mathbf{2676 \text{ kJ}}$$

