170°C

(12 tube passes)

8-88 Water is heated by hot oil in a heat exchanger. The outlet temperature of the oil and the rate of exergy destruction within the heat exchanger are to be determined.

Assumptions 1 Steady operating conditions exist. 2 The heat exchanger is well-insulated so that heat loss to the surroundings is negligible and thus heat transfer from the hot fluid is equal to the heat transfer to the cold fluid. 3 Changes in the kinetic and potential energies of fluid streams are negligible. 4 Fluid properties are constant.

Properties The specific heats of water and oil are given to be 4.18 and 2.3 kJ/kg.°C, respectively.

Analysis We take the cold water tubes as the system, which is a control volume. The energy balance for this steady-flow system can be expressed in the rate form as

$$\frac{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}}{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}} = \underbrace{\Delta \dot{E}_{\text{system}}^{70 \text{ (steady)}}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\Delta \dot{E}_{\text{system}}^{70 \text{ (steady)}}}_{\text{Rate of change in internal, kinetic, potential, etc. energies}} = 0$$

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{Q}_{\text{in}} + \dot{m}h_1 = \dot{m}h_2 \quad \text{(since } \Delta \text{ke} \cong \Delta \text{pe} \cong 0)$$

$$\dot{Q}_{\text{in}} = \dot{m}c_p(T_2 - T_1)$$
Water
$$20^{\circ}\text{C} \longrightarrow 4.5 \text{ kg/s}$$

Then the rate of heat transfer to the cold water in this heat exchanger becomes

$$\dot{Q} = [\dot{m}c_p(T_{\text{out}} - T_{\text{in}})]_{\text{water}} = (4.5 \text{ kg/s})(4.18 \text{ kJ/kg.}^{\circ}\text{C})(70^{\circ}\text{C} - 20^{\circ}\text{C}) = 940.5 \text{ kW}$$

Noting that heat gain by the water is equal to the heat loss by the oil, the outlet temperature of the hot water is determined from

$$\dot{Q} = [\dot{m}c_p (T_{\rm in} - T_{\rm out})]_{\rm oil} \rightarrow T_{\rm out} = T_{\rm in} - \frac{\dot{Q}}{\dot{m}c_p} = 170^{\circ}\text{C} - \frac{940.5 \text{ kW}}{(10 \text{ kg/s})(2.3 \text{ kJ/kg.}^{\circ}\text{C})} = 129.1^{\circ}\text{C}$$

(b) The rate of entropy generation within the heat exchanger is determined by applying the rate form of the entropy balance on the entire heat exchanger:

$$\frac{\dot{S}_{\text{in}} - \dot{S}_{\text{out}}}{\text{Rate of net entropy transfer}} + \frac{\dot{S}_{\text{gen}}}{\text{Rate of entropy}} = \underbrace{\Delta \dot{S}_{\text{system}}}^{\phi 0 \text{ (steady)}}$$
Rate of net entropy transfer Rate of entropy generation Rate of change of entropy
$$\dot{m}_{1}s_{1} + \dot{m}_{3}s_{3} - \dot{m}_{2}s_{2} - \dot{m}_{3}s_{4} + \dot{S}_{\text{gen}} = 0 \text{ (since } Q = 0)$$

$$\dot{m}_{\text{water}}s_{1} + \dot{m}_{\text{oil}}s_{3} - \dot{m}_{\text{water}}s_{2} - \dot{m}_{\text{oil}}s_{4} + \dot{S}_{\text{gen}} = 0$$

$$\dot{S}_{\text{gen}} = \dot{m}_{\text{water}}(s_{2} - s_{1}) + \dot{m}_{\text{oil}}(s_{4} - s_{3})$$

Noting that both fluid streams are liquids (incompressible substances), the rate of entropy generation is determined to be

$$\dot{S}_{\text{gen}} = \dot{m}_{\text{water}} c_p \ln \frac{T_2}{T_1} + \dot{m}_{\text{oil}} c_p \ln \frac{T_4}{T_3}$$

$$= (4.5 \text{ kg/s})(4.18 \text{ kJ/kg.K}) \ln \frac{70 + 273}{20 + 273} + (10 \text{ kg/s})(2.3 \text{ kJ/kg.K}) \ln \frac{129.1 + 273}{170 + 273} = 0.736 \text{ kW/K}$$

The exergy destroyed during a process can be determined from an exergy balance or directly from its definition $X_{\rm destroyed} = T_0 S_{\rm gen}$,

$$\dot{X}_{\text{destroyed}} = T_0 \dot{S}_{\text{gen}} = (298 \text{ K})(0.736 \text{ kW/K}) = 219 \text{ kW}$$